

# Voting and Deliberation

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# REVIEW

Voting and  
Deliberation

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Questions

Gershkov and  
Szentes

Austen-Smith and Feddersen show that in a general setting that a “small” amount of ex ante heterogeneity interferes with honest revelation of information.

# DELIBERATION WORKS, I

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## Preference Uncertainty

Standard binary voting, information environment, but assume that preferences may not be aligned.

For some preferences given by:  $u(a, X) = -.5(a - X)^2$

For others given by:  $v(a, X) = -u(a, X)$

Assume that everything thinks that they are in majority. Full information outcome is equilibrium (in weakly undominated strategies).

Deliberation: Tell Truth.

Voting: Behave sincerely given all information.

Honesty Optimal because you believe that majority will use information "properly."

# DELIBERATION WORKS, II

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## Redundant Information

At least two other people know exactly what you know.  
Under this condition, a voter's behavior is not relevant in a truth-telling equilibrium, so truth-telling is an equilibrium.

# DELIBERATION WORKS, III

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## Extended Preferences

Assume that you can reward people for “correct” information. This can break near indifference and induce revelation.

# ASIDE

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Laslier and Weibull show that informative voting is an equilibrium in a slightly perturbed voting game when the population is large.

Perturbation:

With small probability  $\alpha$  (small) subset of voters determines outcome.

Mechanism is arranged so that agents have incentive to vote honestly.

# BROAD INDIFFERENCE

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Voter behavior makes a difference with small probability, yet conditioning on low probability event (being pivotal) is essential for equilibrium analysis.

Implications for:

- 1 Robustness
- 2 Participation or information acquisition (substantively).  
We should be thinking about reasons why people do participate and how institutional environment matters.
- 3 Equilibrium Refinement (technically)

# ENDOGENOUS INFORMATION ACQUISITION

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- 1  $N$  agents.
- 2 Two actions, states, and signals.
- 3 Symmetric access to information and preferences.
- 4 Information is costly.
- 5 Signal shifts prior from  $.5$  to  $p > .5$ .

# THE PROBLEM

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Design mechanism that maximizes social welfare subject to incentive constraints.

# WHAT IS THE PROBLEM?

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If agents have the same preferences over outcomes, what is the problem?

Information acquisition is a private decision with positive externalities.

People may wish to free ride on the information of others.

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# FIRST BEST: Warm up

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Assume incentive problems do not exist. What is the optimal way to collect information?

Social planner tries to maximize:  $NEu - cL$ , where  $Eu$  is expected payoff and  $L$  is expected number of information purchases.

# COMPUTATION

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Definitions:

$$B(d) = \frac{p^d}{p^d + (1-p)^d}$$

$$R(d) = 1 - B(d)$$

$$p(d) = pB(p) + (1-p)R(d)$$

If you have  $d$  more  $i$  signals than  $j$  signals, then  $B(d)$  is the probability the next signal is  $i$ .

If you have  $d$  more  $i$  signals than  $j$  signals, then  $p(d)$  is the probability that  $i$  is the state.

$d$  is the gap.

# FIRST BEST

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## Proposition

*There exists a decreasing function  $g$  such that  $g(n+1) = g(n)$  or  $g(n+1) = g(n) - 1$ , and  $g(N-1) = 1$ . If, after asking  $n$  voters, make the majority decision if the gap is  $g(n)$ , otherwise continue.*

Solution is sequential sampling.

When you are confident enough, stop.

The earlier you stop, the stronger the evidence needed.

# DYNAMIC PROGRAMMING

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$W(n, d)$  value given  $n$  pieces of information and gap  $d$ , ignoring past information costs.

$$W(N, d) = NB(d)$$

$$W(n, d) =$$

$$\max\{NB(d), p(d)W(n+1, d+1) + (1-p(d))W(n+1, d-1) - c\}$$

- $W(n, d)$  weakly decreasing in  $n$ .  
More strategies with  $n$  low.
- If you stop at  $(n, d)$  you would at  $(n', d)$  for all  $n' > n$ .  
 $W(n, d)$  is decreasing in  $n$ .
- There exists  $f$  such that continue asking if and only if  $n < f(d)$ .
- $f(d) > f(d + 1)$  If you stop at  $(f(d), d)$ , then you must stop at  $(f(d) - 1, d + 1)$  So  $f(d + 1) \leq f(d) - 1$
- $g(N - 1) = 1$   
If  $d > 1$  with one potential observation, the information doesn't influence choice.
- $g(n) = \min\{d : n \geq f(d)\}$  is such that  $g(n) = g(n - 1)$  or  $g(n - 1) - 1$ .

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How does respecting incentive condition change this?  
You need to convince people that their information is  
valuable.  
Keep number of searches secret.

# SEARCH FOR THE OPTIMAL MECHANISM

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Mechanism in a game played by  $N$  agents and nature and an equilibrium of the game.

Note: This is not a standard problem because ex ante agents have no information.

Without loss of generality:

- 1 Mechanism is Sequential with Random Order.
- 2 Agents report information on their moves.
- 3 Agents have trivial information sets.
- 4 Agents acquire information and report in truthfully whenever asked to move.

# WHY?

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Agents have less information than the center.  
Incentive problems milder when people know less.  
Mechanism doesn't tell voter how many others acquired  
information or how they voted.

# INCENTIVE COMPATIBILITY

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Two concerns:

People report truthfully.

People obtain information when asked.

The first is not really a problem. The second is.

When asked, voter must believe that the chances of getting correct answer as the result of an informed vote equal the costs of information.

# OPTIMAL EX POST EFFICIENT MECHANISM

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- Cut off rule qualitatively as before.
- Randomization.
- Agents think that they are decisive with sufficient probability.

# PROPERTIES

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- No information sharing.
- No committees.

# WHAT IS MISSING

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- No joint production or complementarity.
- No differences of opinion.