

## Economics 200C: Problem Set I

Due: April 7, 2004

### Paternalism:

- You've heard me (and others) say that doing problems is really important. There, I said it again.
- Try to make your answers as complete as possible. (Hand waving is for lectures!)
- Clear intuitive statements are better than nothing, but don't forget the previous point.
- If the question is too hard, make stronger assumptions.
- By all means work together. Please write down answers independently (because I think that you'll learn something writing the arguments down).

### Problems:

1. Can a player have two strictly dominant strategies? Give an example or prove that this is impossible.
2. Can a player have two weakly dominant strategies? Give an example or prove that this is impossible.
3. Can adding a strategy for Player 2 increase Player 1's security level? Can it decrease it? Can it increase Player 1's maximum equilibrium payoff? Can it increase Player 1's minimum equilibrium payoff?
4. Can a strategy be strictly dominated by a non-trivial mixed strategy, but not by a pure strategy? Give an example or prove that this is impossible.
5. Can adding a weakly dominated strategy change the set of Nash equilibria in a game? How about adding a strictly dominated strategy?
6. Ten firms must decide whether to operate at location  $A$  or location  $B$ . If there are  $n$  firms in location  $A$ , then each of these firms earns  $n^2$ . If there are  $m$  firms at location  $B$ , then each of these firms earns  $2m^2 - 14$ . Describe the pure-strategy Nash equilibria of the game that arises if the firms simultaneously decide upon a choice of location. Write down (but do not solve) an equation that would characterize a symmetric (all firms play the same strategy) mixed-strategy equilibrium for the game. Show (if you can) that this equation has a solution.
7. Three voters ( $i = 1, 2, 3$ ) must decide between two candidates,  $A$  and  $B$ . The candidate with the most votes wins. Voters 1 and 2 prefer candidate  $A$  to candidate  $B$ . Voter 3 prefers candidate  $B$ . Voters vote simultaneously. Show that there is an equilibrium in which candidate  $B$  wins. Show that this outcome disappears if voters avoid weakly dominated strategies.