## Table 1

Point and Bootstrap Estimates, Educational Spending (x) and Wages (w), Black/White (BW) typology, Average Spending per Pupil $\mathbf{R}=\$ \mathbf{2 , 5 0 0}$ and Minimum Spending per Pupil $\mathbf{x}_{\text {min }}=\$ 2500$ With No Limit on Average Spending $\mathbf{R}$

|  | Average Spending per Pupil R | Spending per Pupil, Blacks $x^{B}$ | Spending per Pupil, Whites $x^{W}$ | Ratio $x^{B} / x^{W}$ | Weekly <br> Wages, <br> Blacks <br> $w^{B}$ | Weekly <br> Wages, <br> Whites <br> $w^{W}$ | Average <br> Wages <br> under <br> Equal <br> Resources <br> $w^{E R}$ | Average Wages under Equal Opportu- nity $w^{E O_{p}}$ | Efficiency <br> Ratio <br> $v$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Average Spending R=2.5 |  |  |  |  |  |  |  |  |  |
| Point estimate | 2.50 | 14.76 | 0.828 | 17.82 | 0.584 | 0.604 | 0.631 | 0.602 | . 953 |
| . 025 estimate | 2.50 | 10.71 | 0.241 | 7.76 | 0.462 | 0.586 | 0.625 | 0.571 | . 905 |
| . 975 estimate | 2.50 | 19.07 | 1.381 | 79.17 | 0.688 | 0.622 | 0.636 | 0.628 | . 944 |


| Minimum <br> Spending per <br> Type $X_{\min }=2.5$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Point estimate | 4.85 | 22.18 | 2.49 | 8.92 | 0.709 | 0.653 | 0.701 | 0.660 | . 942 |
| . 025 estimate | 3.85 | 13.58 | 2.45 | 5.39 | 0.642 | 0.647 | 0.668 | 0.651 | 0.807 |
| . 975 estimate | 8.55 | 53.12 | 2.55 | 21.49 | 1.039 | 0.659 | 0.832 | 0.699 | 1.000 |

Note: All dollar amounts are expressed in thousands of 1990 dollars.

Table 2
Point Estimates and Bootstrap Estimates, Educational Spending $x$ and Wages w, Four-Type Parental Education Typology,
Average Spending per Pupil $\mathbf{R}=\mathbf{\$ 2 , 5 0 0}$ and Minimum Spending per Type $\mathbf{x}_{\text {min }}=\mathbf{\$ 2 5 0 0}$ With No Limit on Average Spending R.

|  |  | Spending per Pupil (1=Lowest Parental <br> Education) |  |  |  | Weekly Wages (1= Lowest Parental <br> Education) |  |  |  | Average Wages |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Average <br> Spending <br> per Pupil <br> R | $\mathrm{X}_{\text {E1 }}$ | $\mathrm{x}_{\mathrm{E} 2}$ | $\mathrm{X}_{\mathrm{E} 3}$ | $\mathrm{X}_{\mathrm{E} 4}$ | $\mathrm{W}_{\text {E1 }}$ | $\mathrm{W}_{\text {E2 }}$ | $\mathrm{W}_{\text {E3 }}$ | $\mathrm{W}_{\text {E4 }}$ | Equal <br> Re- <br> sources <br> $w^{E R}$ | Eqal <br> Oppor- <br> tunity <br> $w^{E O p}$ | Efficiency Ratio $v$ |
| Average Spending per Pupil R=2.5 |  |  |  |  |  |  |  |  |  |  |  |  |
| Point estimate | 2.50 | 5.36 | 3.62 | 1.88 | 1.10 | 0.656 | 0.653 | 0.638 | 0.659 | 0.633 | 0.649 | 1.026 |


| . 025 estimate | 2.50 | 4.47 | 2.87 | 1.34 | 0.22 | 0.605 | 0.616 | 0.620 | 0.641 | 0.627 | 0.635 | 1.007 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| . 975 estimate | 2.50 | 6.28 | 4.20 | 2.21 | 1.14 | 0.670 | 0.674 | 0.647 | 0.692 | 0.638 | 0.655 | 1.034 |
| Minimum Spending per Type $\mathrm{x}_{\min }=2.5$ |  |  |  |  |  |  |  |  |  |  |  |  |
| Point <br> estimate | 4.33 | 7.31 | 4.75 | 3.61 | 2.51 | 0.749 | 0.714 | 0.698 | 0.694 | 0.695 | 0.710 | 1.023 |
| . 025 estimate | 3.58 | 5.44 | 3.69 | 2.60 | 2.45 | 0.657 | 0.663 | 0.662 | 0.682 | 0.665 | 0.675 | 1.004 |
| . 975 estimate | 4.93 | 9.69 | 6.34 | 4.53 | 2.55 | 0.821 | 0.790 | 0.716 | 0.706 | 0.714 | 0.730 | 1.031 |

Note: All dollar amounts are expressed in thousands of 1990 dollars.
$E_{1}=$ parental education less than or equal to eight years
$\mathrm{E}_{2}=8<$ parental education $<12$
$\mathrm{E}_{3}=$ parental education $=12$
$\mathrm{E}_{4}=$ parental education $>12$

Table 3
The Percentage of Black Workers in Each Earnings Quintile in Raw Data and After Various Types of Reallocation of Educational Expenditure

| Description of Allocation | Earnings Quintile (5=Bottom) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 5 | 4 | 3 | 2 | 1 |
| Raw Data | 46.73 | 20.5 | 15.67 | 11.66 | 5.44 |
| Average Spending R = 2.5 for All Workers | 46.44 | 21.59 | 16.77 | 10.38 | 4.82 |
| Equal Opportunity Black/White (EOp B/W), Average Spending R=2.5 | 25.43 | 21.99 | 16.11 | 20.09 | 16.37 |
| Equal Opportunity Black/White (EOp B/W), Minimum Spending perType $x_{\text {min }}=2.5$, Average Spending $R=4.85$ | 34.27 | 14.91 | 8.95 | 13.85 | 28.02 |
| Equal Opportunity (4-type parental education), Average Spending $R=2.5$ | 38.29 | 21.56 | 21.67 | 12.31 | 6.17 |
| Equal Opportunity (4-type parental education), Minimum Spending per Type $\mathbf{x}_{\text {min }}=2.5$, Average Spending $R=4.33$ | 37.96 | 27.37 | 24.19 | 7.38 | 3.11 |

Note: Earnings data are adjusted for variations in earnings by age using regression coefficients from the B/W typology. Quintile 5 refers to the fifth of the population with the lowest earnings. Calculations are based on spending under various equalization and EOp policies and regression coefficients from the B/W typology.

## Table 4

## Estimated Gains in the Objective Function and Costs per Student of Various Interventions Using the Black-White Typology

Note: Estimated cost per person is calculated as total program cost divided by the number of persons in the sample, where costs are calculated as a present value in the year in which the person reaches age 18. The "value of objective function" is derived from the average value of the lower envelope in log weekly wage: $q$ space, re-expressed in average earnings per week for workers on the envelope. N/A: "not applicable".

|  |  |  | P.D.V of |
| :---: | :---: | :---: | :---: |
| Policy Description | Value of Objective | Change Relative to |  |
| Function (\$) | Base Case | Cost per |  |
| Student |  |  |  |
| Base Case, Unequal Resources, Mean Spending=2.5 | $\$ 464.58$ | $\mathrm{~N} / \mathrm{A}$ | N/A |
| Equal Resources, Mean Spending=2.5 | $\$ 465.68$ | $\$ 1.10$ | 0 |
| Equal Opportunity, Mean Spending=2.5 | $\$ 510.91$ | $\$ 46.33$ | 0 |
| Equal Opportunity, Minimum Spending per Type=2.5 | $\$ 530.37$ | $\$ 65.79$ | $\$ 34,597.83$ |

